A novel hybrid optimization methodology to optimize the total number and placement of wind turbines

3 AUTHORS, INCLUDING:

Kishalay Mitra
Indian Institute of Technology Hyderabad
56 PUBLICATIONS   **606** CITATIONS

SEE PROFILE

1

A novel hybrid optimization methodology to optimize the total number and placement of wind turbines

5

Prateek Mittal[1], Kedar Kulkarni[2], Kishalay Mitra[1,*]

[1]Department of Chemical Engineering, Indian Institute of Technology Hyderabad, Ordnance Factory Estate, Yeddumailaram 502205, INDIA

[2]ABB Corporate Research Center, Mahadevapura, Bangalore, 560048, INDIA

10

[*] Corresponding author: e-mail: kishalay@iith.ac.in; Telephone: 914023017055;

11

Abstract

Due to increasing penetration of wind energy in the recent times, wind farmers tend to generate increasing amount of energy out of wind farms. In order to achieve the target, many wind farms are operated with a layout design of numerous turbines placed close to each other in a limited land area leading to greater energy losses due to 'wake effects'. Moreover, these turbines need to satisfy many other constraints such as topological constraints, minimum allowable capacity factors, inter-turbine distances, noise constraints etc. Thus, the problem of placing wind turbines in a farm to maximize the overall produced energy while satisfying all constraints is highly constrained and complex. Existing methods to solve the turbine placement problem typically assume knowledge about the total number of turbines to be placed in the farm. However, in reality, wind farm developers often have little or no information about the best number of turbines to be placed in a farm. This study proposes a novel hybrid optimization methodology to simultaneously determine the optimum total number of turbines to be placed in a wind farm along with their optimal locations. The proposed hybrid methodology is a combination of probabilistic genetic algorithms and deterministic gradient based optimization methods. Application of the proposed method on representative case studies yields higher Annual Energy Production (AEP) than the results found by using two of the existing methods.

Keywords: Wind energy; systems engineering; micro-siting optimization; genetic algorithms; gradient based optimization; hybrid techniques

31

32

1. INTRODUCTION

Wind energy has turned out to be a promising alternative energy source in order to compete with the depleting conventional sources. Due to its wide-scale availability, low cost and environment friendly operation, the idea of utilizing wind power at a massive scale has become a primary focus in the power industry, government policies and academic research [1-3]. According to the Global Wind Energy Council (GWEC) [4], the global cumulative installed wind capacity has increased from 6100 MW to 318,105MW in the last two decades and is expected to reach 1100GW over the next five years (~12% of electricity supply of the world). The standard systems engineering approach of capturing the potential wind energy in a farm is to place wind turbines at optimal locations, known as micro-siting, and thereby tapping the maximum energy out of it. The problem of micro-siting optimization is not trivial due to various challenges involved in problem formulation and development of solution methodology. The challenges related to problem formulation appear while handling different kind of constraints such as inter-turbine distance, topology, overall capacity factor, longevity of turbine life, turbine noise, consideration of turbine wakes etc. While dealing with above constraints, micro-siting problems often lead to mixed integer nonlinear programming (MINLP) formulations for which the methodologies which can guarantee the global solution are yet to be developed. Moreover, the fact that the predictions of the commercial softwares [5-7] for designing the layout of turbines in a wind farm till date are still not up to the mark [2] and human intervention is required to reduce the installation and operational costs, shows the scope of improvement in this field both in terms of development of methodologies for efficient problem formulation and solution technique.

54   A huge amount of work has been done in the area of micro-siting over the past two decades [8-

55 10], where binary-coded Genetic Algorithms (GAs) have been used to maximize the net Annual

56 Energy Production (AEP) with less installation cost over fixed number of turbines in a wind farm.

57 Mossetti's [8] work showed the effectiveness of GA for solving such problems. The results for

58 different wind conditions shown in this work were improved later by Grady [9] by considering a

59 higher population size and number of generations thus allowing candidate solutions to have

60 sufficient time to converge. In the study of Emami and Noghreh [10], the conflict of AEP and the

61 cost involved in the project was expressed in the form of weighted sum of these two objectives and

62 better results were found for certain set of weight values in the objective function. These studies

63 consider a farm of regular shape (rectangle) that can be sub-divided into several cells of the size of

64 five times the rotor diameter of the turbines. Assuming only one turbine can be accommodated in

65 each of these cells, these formulations ensure the turbines are placed sufficiently away from one

66 another to avoid wake effects. Mittal [11] reduced these cell sizes by 40 times and shown the

67 effectiveness of the approach by improving the earlier results [8-9] substantially. Wan et al. [12]

68 used real coded GA to solve the positioning problem of fixed number of turbines and obtained better

69 results as compared to the work of Grady [9]. Mora et al. [13] proposed variable length

70 chromosomes in GA to handle different types of turbines in micro-siting and developed novel

71 crossover and mutation operators to handle these chromosomes of different lengths. Gonzalez et al.

72 [14] proposed another variable length codification in an efficient GA setup to optimize the layout

73 of turbines by calculating net yearly income obtained by selling net energy produced by each turbine

74 considering various kinds of energy losses. The step of codification represents each of the

75 chromosomes as different layouts, where the length of chromosome is driven by the total number

76 of turbines in a farm and information related to turbine attributes is also coded. Apart from GA,

other evolutionary techniques such as Imperialist Competitive Algorithm [15], Strength Pareto Evolutionary Algorithm (SPEA) [16], Ant Colony Optimization [17], Particle Filtering Approach [18], Particle Swarm Optimization [3] etc. were used to deal with the optimal placement of turbines in a wind farm layout and solve different single or multi-objective optimization formulations. In another multi-objective formulation, Kwong et al. [19] considered the maximization of AEP and minimization of the noise level for a fixed number of turbines in a wind farm. Zhang et al. [20] presented Constrained Programming and Mixed Integer Programming models to maximize the total farm-level energy produced for simple to complex wind scenarios. Currently, several commercial software programs are available addressing the problem of wind farm layout and design. The most widely used is WAsP [5], which offers modules that allow assessing wind behavior in complex terrain using computational fluid dynamics (CFD). It helps to develop wind farm design by considering previously obtained wind climate observations and wake effect is calculated using Katic model [21]. Windfarmer [6] optimizes the layout using Reynolds Average Navier-Stokes (RANS) based CFD model. It considers uncertainty, noise, and electrical infrastructure as additional aspects. WindPro [7] designs the layout by sequentially adding the wind turbines at positions with maximum available energy while optimizing the net AEP of a farm.

Most of the existing models and software packages solve the micro-siting problem assuming the total number of turbines in a wind farm is fixed i.e. the rated power capacity of a wind farm is known and the goal here is to find out the turbine locations. In this case, the problem is a nonlinear programming problem, where turbine locations are the only decision variables. Under different circumstances, either the rated power capacity has been driven by certain business decisions or it has been arrived at based on past experiences of the experts. There are issues with either of these approaches. If the rated capacity is higher than the optimal rated capacity (which is unknown and

100   needs to be found out), the rated capacity will be misleading and will never be realizable. On the

101   other hand, if the rated capacity is lower than the optimal value, the purpose of tapping the full

102   potential of wind energy can be jeopardized. However, the optimal rated capacity can be found by

103   formulating an optimization problem which can calculate the total number of turbines that can be

104   placed in a farm layout as well as their locations. A common practice observed in many practical

105   installations is to erect as many turbines as possible in a wind farm ignoring the wake effect and

106   thereby generating an inefficient as well as sub-optimal micro-siting plan. It is, therefore, more

107   realistic to find out the optimal total number of turbines as well as their locations simultaneously

108   while performing micro-siting in presence of several other constraints.

109   Though some of earlier studies address this issue of simultaneous determination of optimal total

110   number and locations of turbines in a wind farm, a severe compromise has been made in terms of

111   assuming the locations of the turbines only at fixed locations. For example, a wind farm is divided

112   into certain number of cells and the center of the cell is assumed to be the only location of a turbine

113   in that cell. No additional constraint for tackling the inter turbine distance has been considered;

114   instead the size of each of these cells is assumed to be some integer times (e.g. five times) the rotor

115   diameter of the turbine. Simultaneous determination of optimal total number and locations of

116   turbines in a wind farm for an objective, say maximization of AEP, involves both binary ("yes / no"

117   decisions for turbines at several locations) and continuous variables (turbine coordinates) and leads

118   to mixed integer (non)linear programming (MINLP) formulations. Assuming the total number of

119   turbines to be installed is N_t and the whole farm area under study is divided into N_{cell} units, the

120   possible number of distinct solutions that has to be considered during optimization can be given by

121   equation (1) [22].

122
$$N_{sol} = \left(\frac{N_{cell}}{N_t} \right) = \frac{N_{cell}!}{N_t!(N_{cell} - N_t)!}$$
(1)

123 The size of the problem and thereby the complexity increase with the increase in number of cells in

124 the search space (the case of division of the wind farm into finer grids) and the problem size could

125 be unmanageable after a certain extent of granularity in the grid / cell size. Recently, Chen et al.

126 [23] adopted a mix of real and binary coded GA to solve this problem where each layout is

127 represented by a triplet of a fictitious number (N_f number for each of them) of x, y coordinates and

128 binary variables. Depending on the number of '1's present in the N_f binaries, the total number of

129 turbines in a layout is calculated whereas their corresponding x and y coordinates are their

130 respective locations in the layout. Since the total number of turbines is not known here, several

131 optimization runs with different values of N_f are recommended. The amount of complexity involved

132 in this formulation can be guessed from the estimates of number of solutions to be considered from

133 (1) since the real values of the coordinates can assume any value within the given bounds. In another

134 study, Kulkarni and Mittal [24] developed a novel heuristic approach, where the optimal number of

135 turbines and their optimal locations can be found out simultaneously in order to maximize the net

136 AEP and minimize the wake losses in a wind farm. It suffers from the drawback of other grid-based

137 methods: since all candidate turbine-locations lie on the grid, possibly better locations lying

138 between grid-points can never be chosen. Moreover, refining the grid resolution to better represent

139 the wind farm area may make the problem computationally very demanding. Another limitation of

140 this approach is that the performance of the algorithm is driven by the selection of the starting

141 solution. To overcome these limitations, a novel hybrid methodology has been proposed in this

142 work which makes use of a bi-level optimization formulation. GA has been used in the first level

143 to determine the number of turbines out of certain number of possible candidate locations (a discrete

144 formulation) whereas a classical optimization technique improves those locations in the second

145 level assuming the number of turbines in the layout as obtained from the first level are fixed (a

146 continuous formulation). This study additionally considers the presence of other constraints such

147 as inter turbine distance, overall capacity factor, presence of wake in energy calculations etc. The

148 rest of the paper has been organized as follows. Section 2 describes the optimization problem

149 formulation while AEP calculation and functioning of the wake model are discussed in section 3.

150 Section 4 explains the heuristic methodology followed by the brief description of the proposed

151 hybrid optimization methodology in section 5. Finally, the results of different representative case

152 studies and the conclusions are presented in the sections 6 and 7 respectively.

153 **2. PROBLEM FORMULATION**

154 The development of mathematical model for wind farm micro-siting is limited to certain

155 assumptions. These assumptions can be modified or even removed as and when needed. The

156 assumptions are described as follows:

157 *Assumption 1:* Wind turbine locations are described by a Cartesian coordinate system (x_i, y_i),

158 $i = 1,...., N$, where N is the number of turbines.

159 *Assumption 2*: Wind turbines are assumed to have uniform specifications in terms of rated power,

160 rotor diameter, hub-height etc.

161 *Assumption 3:* A widely used Jensen wake model [25] is used to calculate the velocity deficit due

162 to wake effects.

8

163   *Assumption 4:* As widely used in literature, the wind speed is assumed to follow a two parameter

164   Weibull distribution [26] $C_v(u, A, k) = 1 - e^{-\left(\frac{u}{A}\right)^k}$, where A is the scale parameter, k is the shape

165   parameter and $C_v(.)$ is the cumulative Weibull distribution function.

166   *Assumption 5:* Power and thrust coefficient curves [30] for a Vestas-V52 850 kW turbine are used

167   to evaluate the power and coefficient of thrust for corresponding wind-speeds (as shown in Fig. 1).

168   Mathematically, the problem can be represented as:

169   *Objective Function*: $\underset{N_t}{Max} \underset{x_i, y_i}{Max} \sum_{1}^{N_t} AEP(x_i, y_i)$

170   *Constraints*: $\begin{aligned} g_j(x_i, y_i) \leq 0, \quad j = 1, ..., Nc; \quad i = 1, ..., N_t \\ lb \leq (x_i, y_i) \leq ub \end{aligned}$ (2)

171   Here, in equation (2) [24], N_t is the total number of turbines, is taken as a *upper level* decision

172   variable and (x_i, y_i), the location co-ordinates of these turbines, are considered as a *lower level*

173   decision variables. Nc denotes the number of constraints, whereas the geographical boundary limits

174   are depicted by lb and ub . For a regular square farm of 500×500 m^2 considered here, the lb and

175   ub for x_i and y_i can be 0 and 500, respectively.

176   The inequalities $g_j(x_i, y_i) \leq 0$, represent the following constraints:

177   i)   Inter turbine distance (ITD), which is kept greater than or equal to 3 times the rotor

178   diameter of the turbines.

179    $$g_1(x_i, y_i) = n_{space} * D - \sqrt{\left(x_i - x_j\right)^2 + \left(y_i - y_j\right)^2} \leq 0,$$ (3)
       $$j = i, j; j = 1, ..., N_t$$

9

180   ii)   Overall capacity factor (OCF), which is kept to be higher than the specified limit for it

$$g_2(x_i, y_i) = OCF^{\text{lim}} - \frac{\sum\limits_{1}^{N_t} AEP(x_i, y_i)}{(8766) * N_t * \text{Pr}} \tag{4}$$

181

182   In the above equations (3 and 4), D is the rotor diameter of turbine, n_{space} is the minimum

183   allowable distance between two turbines which is assumed to equal to 3, OCF^{lim} is the selected

184   limit of allowable capacity factor which is assumed to be 20% and Pr is the rated power (850kW)

185   of a wind turbine. These inequality constraints are explained briefly in section 5. The above problem

186   belongs to the class of mixed integer nonlinear programming problems (MINLP) that are generally

187   very hard (NP-hard) to solve due to the combinatorial complexity involved.

188   **3. AEP CALCULATION AND WAKE MODELING**

189   *3.1. AEP Calculation*

190   To calculate the net energy produced accurately, the spatial and temporal distribution of wind

191   resource must be known which is generally expressed in terms of wind resource grid (WRG) that

192   stores information about Weibull parameters at a given location. The net AEP (kWh) at a given

193   location of wind farm can be expressed as [26]:

$$AEP = (8766) \sum_{i=1}^{directions} \sum_{j=1}^{speed} \sum_{k=1}^{turbines} Frequency_{ijk} \ Power_{ijk} \tag{5}$$

194

195   where, $Frequency_{ijk}$ is the frequency or probability of wind coming from direction i, with wind

196   speed j on to the turbine k, and similar terminology holds for $Power_{ijk}$ in kilowatts (KW).

197   Practically, the above formula can be approximated as [16]:

10

$$AEP = (8766) \sum_{i=1}^{360^{\circ}} \sum_{j=1}^{u_{max}} Pwr(\theta_i, u_j) \; p(\theta_i) \; p(u_j) \Delta\theta_i \; \Delta u_j \qquad (6)$$

199   where $p(\theta_i)$ and $p(u_j)$ determine the probability that the wind blows in direction θ_i at speed u_j

200   and are obtained from WRG data. Depending on whether a turbine is affected by wake and the

201   number of upstream turbines generating the wake, the reduced speed at the turbine affected by

202   wake is calculated. The corresponding power $Pwr(\theta_i, u_j)$ for that particular speed can be

203   calculated using the turbine power curve (see Fig.1). The two-parameter Weibull distribution is

204   used to calculate the $p(u_j)$ by using equations (7) and (8) [30].

$$W_{cum}(u, A, k) = 1 - e^{-\left(\frac{u}{A}\right)^k} \qquad (7)$$

$$p(u_j) = Wcum\left(u_j + \frac{u_{step}}{2}, A, k\right) - Wcum\left(u_j - \frac{u_{step}}{2}, A, k\right) \qquad (8)$$

207   Where W_{cum} is the cumulative probability distribution and $p(\theta_i)$ is extracted from parameter f given in

208   WRG for a particular location.

209   *3.2. Wake model and calculation*

210   In a wind farm, different turbines interact with each other due to wake effects that upstream

211   turbines create on downstream turbines. Among various wake models reported in the literature, a

212   widely accepted Jensen wake model [25] has been adopted here. An expression for the reduced

213   wind-speed of downwind turbines due to wake-effects can be expressed as follows:

$$\Delta u_{ij} = u_o \left(1 - \sqrt{1-C_T}\right) \left(\frac{R_o}{R_o + k_w * d_{ij}}\right)^2 \left(\frac{A_{ij}}{A_j}\right) \tag{9}$$

The following nomenclature is followed in the above equation assuming i and j as upwind and downwind turbines, respectively.

Δu_{ij} : Reduction in the wind speed on turbine j due to the turbine i,

u_o : Free stream wind speed,

C_T : Coefficient of thrust (Fig. 1),

R_o : Rotor radius,

k_w : wake decay constant for Jensen model,

d_{ij} : Distance between upstream and downstream turbines (see Fig. 2),

A_{ij} : Overlapped area [3] varies depending on type of wake effect on downwind turbine and

A_j : Downwind turbine area.

Fig. 2 depicts the variation in distance calculation due to three types of wake effects. Here, R_r is the rotor radius of downwind turbine and R_{ij} is the wake radius created by an upwind turbine on the downwind. Depending on the area overlapped, the distance between two turbines d_{ij} is calculated.

In reality, a downwind turbine may be under the influence of multiple upwind turbines. In that case, equation (9) can be modified as follows:

231
$$U_j = u_o \left(1 - \sqrt{\sum_{k=1, k \neq j}^{N_{upwind}} \left(\Delta u_{ij} \right)^2} \right)$$
(10)

232   where, U_j is the effective wind-speed at turbine j while accounting for all wake effects and N_{upwind}

233   is the number of upwind turbines. Speed deficit, Δu_{ij} in equation (10), is a function of location

234   coordinates as well as wind directions [15 and 24].

235   **4.   HEURISTIC APPROACH**

236   In the heuristics methodology of Kulkarni and Mittal [24], the given square layout is divided

237   into a fine grid and the points where the grid lines cross each other can be considered as possible

238   turbine locations. Subsequently, turbines are placed in these possible locations one by one starting

239   with the point where the gross AEP is maximum. The subsequent turbines are placed at locations

240   where AEP will be the best and none of the constraints such as ITD, OCF will most likely be

241   violated. The algorithm is implemented as follows. In the first step, a point is selected based on

242   the gross AEP and added to the accepted turbine location matrix (M). In the next step, other

243   locations surrounding the accepted location and violating other constraints are discarded and are

244   added up to the rejected turbine location matrix (V). The left over locations are next updated as

245   available locations. Now, the next turbine can again be added at the location that shows highest

246   gross AEP value in the map and no constraint violation among all available locations. This way of

247   adding turbines is continued till the search on all possible candidate locations is exhausted. Fig. 3

248   shows the schematic view of this methodology. It can be seen that the matrices M and V are

249   updated at each iteration. In this fashion, the total number of turbines and their respective locations

250   can be found out in one shot. As explained earlier, the above mentioned heuristic approach [24] of

251   determining the optimal number as well as location of turbines in a farm layout has a drawback of

13

252 lack of continuity i.e. the turbines can only have certain available locations for the optimal

253 placement. This is because the heuristic algorithm discretizes the given geographical boundary

254 into finite number of grid-points, and the grid-cross sites act as the only possible locations for

255 candidate turbines. Therefore, the turbines can be placed only in those available locations leaving

256 the scope of any other nearby points to be one of the optimal points. Also, the heuristic

257 methodology lacks the stability, since outcomes can be different depending on the selection of the

258 starting point. Due to lack of stability, it might be difficult for wind farm developers to decide on

259 which starting point to start the search process of locating the turbines using the heuristic approach

260 and this shows that the practical application of this approach could be limited. However, the results

261 generated by the heuristic approach can be used as an intelligent initial guess to other

262 methodologies.

263 **5. HYBRID METHODOLOGY**

264 To overcome the drawbacks in the heuristic approach, a novel hybrid methodology is

265 developed to determine the optimal number and location of turbines, simultaneously. The proposed

266 hybrid approach is a combination of probabilistic GAs and deterministic gradient search based

267 methods. The problem of simultaneous determination of optimal number and layout of turbines is

268 decomposed into two sub-problems that can be solved in sequence. In the first step, the regular

269 square wind farm is converted into a finite number of grid points and the optimal turbine number

270 and locations are simultaneously determined from a selected finite number of possible locations

271 (grid cross points) through GAs. In the second step, the turbine number is fixed at the value obtained

272 in the first step and the turbine co-ordinates are improved through classical gradient-based

273 optimization techniques. The first sub-problem solves an integer programming problem over the

274 possible turbine locations (the grid cross-points) through binary variables 0 and 1 signifying

275 absence and presence of turbine at different locations, respectively. Based on number of possible

276 locations, the total number of binary variables are determined. The second sub-problem is a

277 continuous nonlinear programming problem where the total number of turbines is fixed, as

278 determined in the first step, and the focus is on determining optimal turbine coordinates given the

279 total number of turbines. The proposed hybrid methodology can start the search procedure using

280 one of the feasible heuristic outcomes [24] as initial guess and the cycle between evolutionary and

281 gradient approach (Fig. 4) is continued until a predefined termination criteria is met. The proposed

282 hybrid methodology comprises five important components.

283 *5.1.Feasible initial guesses through heuristics*

284   GA needs an initial population which can be generated randomly as well as using the afore-

285 mentioned heuristics (section 4). It can help the algorithm to converge faster if feasible initial

286 guesses can be provided as compared to starting with different random infeasible guesses

287 especially when the search space is huge. Hence, different feasible layouts with different starting

288 points in the heuristic algorithm can be used as initial population of GA.

289 *5.2. Grid Formation*

290   The square (500 × 500 m^2) wind farm is converted into a finite number of grid-points (7×7)

291 leading to 49 possible locations for turbines. Though grids are formed for both approaches, grid

292 resolution of heuristic approach and hybrid methodology are not necessarily the same. So, the final

293 solutions of the heuristic approach may not belong to the set of grid points of the GA. After

294 obtaining a heuristic outcome (say 8 turbines can be feasibly located), the starting matrix of

295 candidate turbine location in GA is formed by adding these 8 locations to 49 grid cross points

296 when there is no points common between them. Using these 57 locations, a *location index array*

297   with unique index for each location is formed (Fig. 5). Each location can be represented by 0 or 1

298   depending on the absence or presence of turbines in that location, respectively (*binary array*).

299   *5.3.Evolutionary Algorithm*

300   An elitist version of binary coded genetic algorithm has been used here. Evolutionary algorithm

301   is a combination of several steps which is described in Fig. 6.

302   *Step I (Initialization):*

303   First, an initialization matrix of n_{pop} x 57 size has been formed (as shown in Fig 7) where one of

304   the chromosomes would be a feasible heuristic outcome and others are generated randomly.

305   Different GA parameters can be found in Table 1.

306   *Step II (Modified Function Evaluation):*

307   The constrained optimization problem has been converted into an unconstrained optimization

308   problem in order to reduce the complexity of constraint handling in GA. The constraints are first

309   normalized and added to the objective function to form a modified unconstrained objective

310   function that can be represented as:

311 $$\textit{Modified obj.} : \underset{N_t}{Max} \underset{x_i,y_i}{Max} \sum_{1}^{N_t} AEP(x_i, y_i) - NormConstraints \tag{11}$$

312   Here, *NormConstraints* is a summation of all inequality constraints that are normalized to represent

313   them into a scale of similar order of magnitude. As our main objective is to maximize both the

314   number of turbines as well as the net AEP, *NormConstraints* are subtracted from the objective

315   function to obtain the modified objective function. In this way, when a particular constraint is

316   violated, the amount of normalized constraint violation is subtracted from the objective function

317 to lower the value of the modified objective function. Objective function is not modified when a

318 particular solution is feasible. These constraints are explicitly defined as:

319 *Inter turbine Distance (ITD)*: In order to lessen the wake loss and alleviate the fatigue loads,

320 enough spacing can be provided between two turbines and the constraint in a normalized form can

321 be represented as:

322
$$g_1(x_i, y_i) = \max\left[0, \left(\frac{n_{space} * D}{\sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}} - 1\right)\right] \qquad (12)$$

323 where, (x_i, y_i) and (x_j, y_j) denotes the location coordinates of upwind and downwind turbines,

324 n_{space} is the minimum distance between two turbines (taken here as 3) and D is the rotor diameter

325 of a turbine (considered here as 52m) (Table 1).

326 *Overall Capacity Factor (OCF)*: Due to various factors such as wind speed reduction, varying

327 wind direction etc., the overall farm capacity is generally lower than the defined theoretical

328 capacity. This constraint is defined in order to measure the wind farm performance. In normalized

329 form it is expressed as:

330
$$g_2(x_i, y_i) = \max\left[0, \left(OCF^{\lim} / \left(\frac{\sum_1^{N_t} AEP(x_i, y_i)}{(8766) * N_t * \Pr}\right) - 1\right)\right] \qquad (13)$$

331 The calculated farm capacity is kept greater than a selected limit value of OCF, called $OCF^{\lim}$,

332 which is taken as 20% in this study.

333   *Topological Constraints*: This constraint is added only to ascertain that the turbines locations lie

334   inside the given geographical boundary and expressed as:

335
$$g_3(x_i, y_i) = \frac{1}{x_{\max}} \sum_{1}^{N_t} \max(-x_i, x_i - x_{\max}, 0) + \frac{1}{y_{\max}} \sum_{1}^{N_t} \max(-y_i, y_i - y_{\max}, 0) \leq 0 \tag{14}$$

336   Here x_{max} and y_{max} are the maximum value on x-axis and y-axis, respectively. In this study, both

337   of these bounds equal to 500 that are given as the geographical limits of square wind farm.

338   After modifying the objective function for each chromosome, the corresponding modified function

339   value is calculated and stored in the initialization matrix as an additional column.

340   *Step III (Crossover and mutation)*:

341   The current population (called as 'parents') undergoes the cross-over and mutation [28] with

342   defined parameters (Table 1) to generate a new set of solutions (called the 'children'). Following

343   the elitist strategy, both these populations are merged together ($2n_{pop}$) and tournament selection

344   is used to obtain the better chromosomes (n_{pop}) among them. Next the initialization matrix is

345   updated and the process continues till the convergence is attained.

346   *5.4. Gradient Based Approach*

347   Though GA can solve the problem of optimal number and location of turbines simultaneously,

348   it performs a search for certain number of fixed locations (grid cross points). If GA is employed

349   to solve the problem with finer grids, the size of the problem (number of binaries) increases with

350   increase in number of grid cross sites, thereby making the GA runs computationally more

351   expensive. The first sub-problem involving GA should, therefore, be solved for a relatively coarser

352   grid which can later be fine-tuned by solving the second sub-problem over the continuous x-y

353 coordinate space. Finally, GA declares the chromosome with the maximum modified function

354 value among all generations as the final solution. The final GA outcome of a feasible layout is next

355 passed as an initial guess to a gradient based solver. A well-known constrained nonlinear

356 optimization routine of MATLAB®, 'fmincon', (Table 1), has been utilized for this purpose. In

357 this step, the only decision variables are location coordinates of the turbines keeping the total

358 number of turbines as constant and the search is performed between the upper and lower bounds

359 of regular square boundary. Since a continuous optimization problem is solved in this step, it

360 searches for coordinates in addition to the points present on the grid for which further improved

361 AEP can be obtained.

362 *5.5. Grid Increment*

363 As mentioned in the section above, the outcomes of the gradient based search method can bring

364 in coordinates that may not be present in the set of grid cross sites that GA uses. As the last step

365 in the hybrid approach, these additional coordinates are added into the candidate location matrix

366 and the index matrix is updated accordingly. This is done to provide more coordinate locations to

367 be searched for GA in the next turn. For example, if the number of old locations were 57 and

368 gradient search provided (say 10) new locations as outcome, the new index array will have total

369 67 locations which are uniquely indexed (Fig 8). After an updated index matrix is obtained, GA

370 run is performed again using the new index array. Further, the outcome of GA is passed as a

371 starting point to gradient based approach and the cycle is continued until a stabilized AEP is

372 obtained as well as the location coordinates for three consecutive iterations are not changed.

373 As mentioned in the beginning of the section, the previous five steps are part of the elitist

374 genetic algorithm (EGA). Few steps are modified in the above approach, called modified EGA

375 (MEGA) as described below, to improve the execution time as well as efficiency of the algorithm.

376   *5.6. Modified Approach*

377   As computation of AEP is found to be the most time expensive step in the algorithm, avenues

378   were sought that can save significant computation in terms of computing AEP selectively. In EGA,

379   AEP was calculated for all the chromosomes in a population. As opposed to that, AEP was

380   calculated for only a part of the population in MEGA. The whole population is partitioned into

381   several sections based on the criteria of constraint satisfaction. If carefully watched, the constraint

382   ITD does not involve AEP computation. ITD computation for the entire population, is, therefore,

383   allowed. Chromosomes in the population for which this constraint (ITD) is unsatisfied, are

384   assigned a flag (say flag 1). Rest of the chromosomes, which satisfies ITD, are further checked

385   their satisfaction of the other constraint, say OCF. Since computation of OCF also involves

386   evaluation of AEP, no more AEP function calls can be saved. However, for implementing another

387   tournament selection based better constraint handling scheme, the population is further classified

388   into different categories. Chromosomes that satisfy the constraint OCF are flagged as 3 and rest of

389   the chromosomes which does not satisfy OCF are flagged as 2. From the above classification, it is

390   clear that the feasible chromosomes are flagged as 3 and chromosomes with other flags violate

391   either of the constraint. This classifies the entire population into feasible and infeasible solutions.

392   While conducting the tournament selection next, chromosome with flag 3 is always allowed to win

393   over chromosomes with any other flag, when two of such chromosomes are picked up randomly.

394   Upon comparison between chromosomes with flag 1 (violating ITD) and flag 2 (violating OCF),

395   one of the chromosomes is picked up randomly. If both the chromosomes with flag 3 are picked,

396   the chromosome with better AEP wins, whereas in case of both the flag to be 1 or 2, the

397   chromosomes with lesser constraint violation is chosen.

6. RESULTS AND DISCUSSIONS

The optimal total number of turbines and their locations have been determined while maximizing the net AEP in a wind farm under several constraints such as inter turbine distance, overall capacity factor and the effect of wakes on the turbines. A hybrid methodology is proposed to overcome the drawbacks of recently developed heuristic approach [24] to solve this problem. The proposed methodology utilizes the merits of probabilistic GA and deterministic gradient based approach to solve this problem. Due to the presence of wake effects, the energy terrain of the problem becomes extremely nonlinear with the gradual addition of turbines into the wind farm. Fig. 9 depicts evolution of the complex and non-linear energy terrain as turbines are successively added to the search space. This set of figures has been generated in this fashion: first, the given layout is discretized into fine grids (say, 101×101 as discussed in section 4). To see the energy terrain in presence of say n+1 turbines, n turbines are placed at certain known locations and the location of the last turbine is varied one by one in leftover available discretized locations and the value of net AEP is captured and depicted through surface-contour plots. For example, Fig. 9a shows the net AEP terrain for two turbines – here the energy surface is generated by keeping the location of one turbine fixed and varying the location of the other turbine across all other locations except the location of the first turbine. As the number of turbines is increased, the complex distribution of net AEP (appearance of several local optima) and increase in non-linear behavior of the problem can be observed from Figs 9b and 9c. In the hybrid methodology suggested here, the classical optimization technique provides the ability to find the optimum more precisely once the near global basin is identified by GA.

As discussed in the following paragraphs, three different case studies with different wind conditions were considered for micro-siting optimization using the proposed hybrid optimization

21

421   method. These case studies differ from one another in terms of the gross AEP distributions over

422   the given geographical boundary. Information regarding these case studies is provided in Table 2.

423   In every case study, the outcome from the heuristic algorithm [24] (H0) is added as one of the

424   chromosomes in the initial population for MEGA and rest of the chromosomes are created

425   randomly. The outcome of MEGA (A1) is passed as an initial guess to the gradient based approach

426   (B1) which improves locations of the turbines further with better net AEP. This cycle between

427   MEGA and gradient-based approach is continued until the change in AEP between two

428   consecutive runs is less than a predefined tolerance. All reported simulations are performed on

429   Intel® Xeon® CPU E5-2690 0 @ 2.90GHz (2 processors) 128 GB RAM machine.

430   *6.1. Case 1: Type – I Gross AEP distribution*

431   The first case study is about a wind farm with complex and non-uniform distribution of wind

432   speed and Gross AEP. It has been assumed in this case that the wind is flowing in uncertain

433   direction at uncertain speed at every location (as shown in Fig. 10). It has been found that heuristic

434   approach [24] on this energy distribution map is able to place 3 turbines while proposed hybrid

435   methodology is able to place 4 turbines with ~44% improvement in AEP as presented in Table 3.

436   The justification of hybrid approach for micro-siting is clearly seen from the results as both the

437   algorithms i.e. MEGA and 'fmincon' are observed to contribute in the net AEP improvement.

438   Improvement in AEP for cases when total number of turbines is fixed (e.g. see the improvement

439   in AEP values from cycle 1 Gradient to cycle 2 MEGA) can be attributed to the detection of better

440   turbine locations. Fig. 11 shows the final superimposed accepted coordinates and number of

441   turbines (black cross markers) on the gross AEP contour plot obtained for the given boundary. As

442   can be observed, the algorithm manages to place only a few turbines in the given layout. The

443   optimal placement of turbines towards one of the boundaries can be attributed to the higher AEP

444 values available along that boundary. This particular case has been generated in such a way that

445 the parameter *A* of Weibull distribution (see assumption 4 in section 2) has zero values in all

446 locations in the given layout except having some nonzero values along the mentioned boundary.

447 More than four turbines are not possible to be placed along that boundary due to violation of ITD

448 constraints.

449 *6.2. Case II: Type – II Gross AEP distribution*

450   In this case study, a uniform distribution of gross AEP is considered across all locations except

451 one location where the wind speed is considered to be higher (Fig. 12). In Fig 12, the location with

452 a higher wind speed is represented by a bump whereas other locations with a negligible amount of

453 gross AEP variation are represented by a flat surface. It has been found that heuristic algorithm is

454 able to place 8 turbines under these wind conditions whereas the proposed hybrid methodology is

455 able to place 12 turbines with ~51% improved in net AEP (Table 4). As can be observed, both

456 MEGA and 'fmincon' efficiently increase the total turbine number and / or the AEP. Fig. 13a,

457 shows the final accepted 12 turbine locations (black cross markers) superimposed on Type –II

458 gross AEP contour plot for the given area. One of the challenging parts of the problem to handle

459 increasing number of binary variables as more number of cycles are completed is also visible from

460 this example (last column of Table 4), which has been successfully handled by GA.

461 *6.3. Case III: Type – III Gross AEP distribution*

462   In this case study, Gross AEP distribution is generated as combination of previous two case

463 studies. Here, the complex Gross AEP distribution is considered in such a way that a particular

464 location in the wind farm gets a higher wind speed and rest of the locations have a disturbed, non-

465 uniform wind flow (see Fig. 14). It has been found that heuristic algorithm alone can place 9

466 turbines in the wind farm whereas the proposed hybrid methodology can place 12 turbines with

467 ~30.25% improvement in the net AEP (Table 5). Though the final number of turbines is the same

468 as the previous case study (Case II), the locations for the turbines are different (Fig. 13). Fig. 13b

469 depicts the final turbine locations superimposed on gross AEP contour plot of Type –III.

470   For all three case studies, the net AEP generated (case 1: 865.95 kWh, case 2: 2054.43 kWh

471 and case 3: 2058.81 kWh) are individually better than the net AEP values obtained by the heuristic

472 algorithm working alone for them. At the same time, it can be observed that AEP improvement by

473 MEGA is further improved by 'fmincon' until convergence, thus establishing the importance of a

474 hybrid algorithm. In other words, using MEGA or 'fmincon' alone will not yield the best possible

475 AEP. Moreover, the MEGA approach is observed to work to the extent of twice as fast as the EGA

476 algorithm for the test cases discussed. Table 6 shows the examples of savings in function

477 evaluation during the calculation of expensive AEP function for each of the cases discussed earlier

478 (23, 52 and 39 % for case1, case 2 and case 3, respectively) which makes MEGA approach more

479 efficient than EGA. As evident, the fastness in obtaining the solution is due to the time saving in

480 the expensive AEP calculation.

481 *6.4. Case IV: A benchmark case study*

482 In order to validate the proposed hybrid optimization approach, a popular case study [9] of uniform

483 wind direction at a speed of 12m/s (see Fig. 16) has been considered next. In this case, similar

484 characteristics of wind farm, wind turbines, power curve and wake model as given in [8] are used

485 (see Table 7) and micro-siting has been performed on this layout using the hybrid optimization

486 approach. The main objective is to minimize the ratio (COST/P_{tot}) i.e. attain the maximum energy

487 throughput (P_{tot}) at minimum COST, while satisfying the ITD constraint of 5D or 200m to

488   minimize the wake effects [9]. Here, COST and P_{tot} is given by equations 15 and 16 and the

489   constraint of ITD (equations 3 and 12) is modified with a new value of n_{space} of 5D [8, 9 and 12].

490
$$COST = N\left(\frac{2}{3} + \frac{1}{3}e^{-0.00174N^2}\right)$$
(15)

491
$$P_{tot} = \sum_{s=1}^{states} \sum_{k=1}^{N} Power_{sk}\ Frequency_{sk}$$
(16)

492   Here, N is the total number of turbines, states are the wind conditions in terms of direction and

493   speed for a particular case study as given in [8], *Power* is defined by power curve [23] and

494   *Frequency* is the occurrence of wind at a particular state [9 and 23]. After evolving the MEGA for

495   2100 generations over 150 population size, the outcome of the hybrid algorithm is compared with

496   other existing methods [8, 9, 12, and 23] and the results are presented in Table 8. It has been found

497   that the hybrid approach is able to place more number of turbines inside the layout as compared to

498   the previous approaches [8, 9 and 12] with better ratio of (COST/P_{tot}) (Table 8) and the results are

499   quite close to the same obtained by Chen et al. [23]. Figure 17 shows the different layouts of

500   turbines obtained by various optimization methodologies for this case study. Table 9 shows the

501   improvement in AEP and convergence of the hybrid algorithm as it marches through the different

502   cycles.

503   Motivated by the approach adopted by Chen et al. [23], which shows improvement in the

504   above case study, where a mix of real and binary coded GA has been used to tackle binary and real

505   variables simultaneously, micro-siting for wind layout with conditions as presented in case 2 has

506   been carried out next. Here a generic GA code has been developed (named as RBGA) where the

507 total number of turbines are fixed to any assumed value (e.g. $N_f = 20$) and the turbine coordinates

508 of these N_f turbines are represented as real variables and existence of turbines in those N_f locations

509 are represented as binary variables (zero for absence and one for presence). This leads to a total of

510 60 decision variables where 40 such variables are x-y coordinates of turbines and 20 variables are

511 binary numbers. Using SBX and polynomial mutation operators for real coded GA [28] and similar

512 operators as MEGA for binary variables, RBGA has been developed. This approach uses binary

513 tournament selection and elitist strategy as adopted in NSGA II [28]. As the MEGA component of

514 the hybrid approach ran for 6 cycles each with 50 population and 150 generations (see Table 4) to

515 generate the final results for case 2, RBGA has been allowed to run for a similar number of

516 generations ($150 \times 6 = 900$) with population 50. RBGA could place 9 turbines altogether in the

517 given layout and Fig. 15 shows the final superimposed accepted coordinates and number of

518 turbines (black cross markers) on the gross AEP contour plot. This is slightly better than the results

519 of the heuristic approach (~ 23.16 % improvement in AEP over heuristic approach) which could

520 place 8 turbines in the same layout; however, this is inferior to the results of the hybrid approach

521 which could place 12 turbines in the same layout (~ 22.61 % improvement in AEP over RBGA

522 approach). This shows the superiority of this hybrid approach over two of the existing approaches

523 [23, 24] in the literature.

524 **7. CONCLUSIONS**

525   Simultaneous maximization of total number of turbines and the net AEP has been carried out

526 for a given wind farm using a novel hybrid optimization strategy. The presence of various types

527 of constraints such as inter turbine distance, overall capacity factor and wake effects have also

528 been considered while conducting the above mentioned micro-siting study. Binary decisions

529 depicting the presence or the absence of turbines across several grid cells in the given regular wind

26

530   farm and the continuous nature of coordinate variables make the formulation a complicated mixed

531   integer nonlinear programing problem. The proposed hybrid methodology is based on the

532   decomposition of the decision variable set into real and binary parts and utilizes the merits of both

533   GA and gradient based approaches to solve this NP-hard MINLP problem. The first sub-problem

534   solves the optimal number and location problem together for selected number of possible locations

535   using GA whereas the second sub-problem improves the coordinates over the continuous

536   coordinate space by keeping the total number of turbines fixed as obtained by the first sub-problem.

537   The proposed methodology is applied to three different wind farm conditions and it has been

538   shown that the proposed methodology works better (~44%, ~51% and ~30% improvement in the

539   net AEP over the heuristics approach) than two of the existing approaches in the literature. This

540   solution methodology can not only help the wind farm developers to find out turbine locations

541   optimally in a given wind farm but also find out the maximum number of turbines that can be

542   optimally fitted in the wind farm simultaneously.

543

544 **8. REFERENCES**

[1]   Duan B, Wang J, Gu H. Modified genetic algorithm for layout optimization of multi-type wind turbines. Proceedings of American Control Conference. 2014, p. 3633-38.

[2]   Khan SA, Rehman S. Iterative non –deterministic algorithms in on – shore wind farm design: A brief survey. Renew Sustain Energy Rev 2013;19:370–84.

[3]   Chowdhary S, Zhang J, Messac A, Castillo L. Unrestricted wind farm layout optimization (UWFLO): Investigating key factors influencing the maximum power generation. Renew Energy 2012;38:16-30.

[4]   Global Wind Report 2013 -Annual Market Update. Available from: < http://www.gwec.net/   publications/global-wind-report-2/global-wind-report-2013/>.[Accessed October 2014].

[5]   WAsP – the Wind Atlas Analysis and Application Program. Available from: <www.wasp.dk/>. [Accessed August 2014].

[6]   WindFarmer. Available from: <http://www.glgarradhassan.com/en/ software/ GHWind Farmer.php>. [Accessed August2014].

[7]   WindPro – EMD. Available from :< www.emd.dk/windpro/>. [Accessed August 2014].

[8]   Mosetti G, Poloni C, Diviacco B. Optimization of wind turbine positioning in large wind farms by means of a genetic algorithm. J Wind Eng Ind Aerodyn 1994;51(1),105-16.

[9]   Grady SA, Hussaini MY, Abdullah MM. Placement of wind turbines using genetic algorithms. Renew Energy 2005;30(2):259-70.

[10]   Emami A, Noghreh P. New approach on optimization in placement of wind turbines within wind farm by genetic algorithms. Renew Energy 2010;35(7):1559-64.

[11]   A. Mittal. Optimization of the layout of large wind farms using a genetic algorithm. Case Western Reserve University; 2010.

[12]   Wan C, Wang J, Yang G, Zhang X. Optimal siting of wind turbines using real- coded genetic algorithms. Proceedings of European wind energy association conference and exhibition. 2009.

[13]   Mora JC, Baron JMC, Santos JMR, Payan MB. An evolutive algorithm for wind farm optimal design. Neurocomputing 2007;70(16-18):2651-58.

[14]   Gonzalez JS, Rodriguez AGG, Mora JC, Santos JR, Payan MB. Optimization of wind farm turbines layout using an evolutive algorithm. Renew Energy 2010;35(8):1671-81.

[15]   Kiamehr K, Hannani SK. Wind farm layout optimization using imperialist competitive algorithm. J Renew Sustain Energy 2014;6(4):043109.

[16] Kusiak A, Song Z. Design of wind farm layout for maximum wind energy capture. Renew Energy 2010;35(3):685-94.

[17] Eroglu Y, Seckiner SU. Design of wind farm using ant colony algorithm. Renew Energy 2012; 44:53-62.

[18] Eroglu Y, Seckiner SU. Wind farm layout optimization using particle filtering approach. Renew Energy 2013;58:95–107.

[19] Kwong WY, Romero D, Zhang PY, Moran J, Morgenroth M, Amon C. Multi objective Wind Farm Layout Optimization Considering Energy Generation and Noise Propagation with NSGA-II. J Mech Des 2014;doi:10.1115/1.4027847.

[20] Zhang PY, Romero DA, Beck JC, Amon CH. Solving wind farm layout optimization with mixed integer programs and constraint programs. EURO J Comput Optim 2014;2(3):195-219.

[21] Katic I, Hojstrup J, Jensen NO. A simple model for cluster efficiency. Proceedings of the European Wind Energy Association Conference and Exhibition. 1986,p. 407-10.

[22] Gonzalez JS, Payan MB, Santos JMR, Gonzalez-Longatt, F. A review and recent developments in optimal wind-turbine micro-siting problem," Renew Sustain Energy Rev 2014;30:133-44.

[23] Chen K, Song MX, Zhang X. Binary-real coding genetic algorithm for wind turbine positioning in wind farm. J Renew Sustain Energy 2014;6:053115.

[24] Kulkarni K, Mittal P. Fast and effective algorithm to optimize the total number and placement of wind turbines. Proceedings of IEEE GHTC-SAS. 2014, p. 7-12.

[25] Jensen NO. A Note on Wind generator interaction. Roskilde, Denmark: Risø National Laboratory;1993

[26] OPENWIND: Theoretical basis and validation. Available from:< http://www.awsopen wind .org/ downloads/documentation>. [Accessed July 2014].

[27] Feng J, Shen WZ. Wind farm layout optimization in complex terrain: A preliminary study on a Gaussian hill. J Phys: Conf Ser 2014;524:012146.

[28] Deb K. Multi-objective Optimization using Evolutionary Algorithms. Wiley, Chichester, UK, 2001.

[29] Vestas-V52 850 KW – Turbine. Available from:< http://en.wind-turbinemodels.com /turbines/71-vestas-v-52>.[Accessed March 2014].

[30] Advance Energy Estimations. Available from:< http://docslide.us/documents/ advanced-energy-estimations-project-hunflen-sweden.html>. [Accessed March 2015].
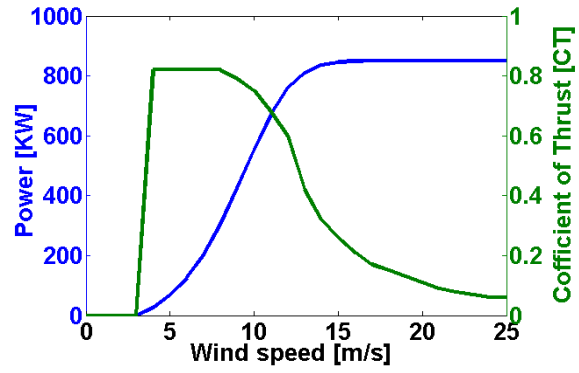
545

546

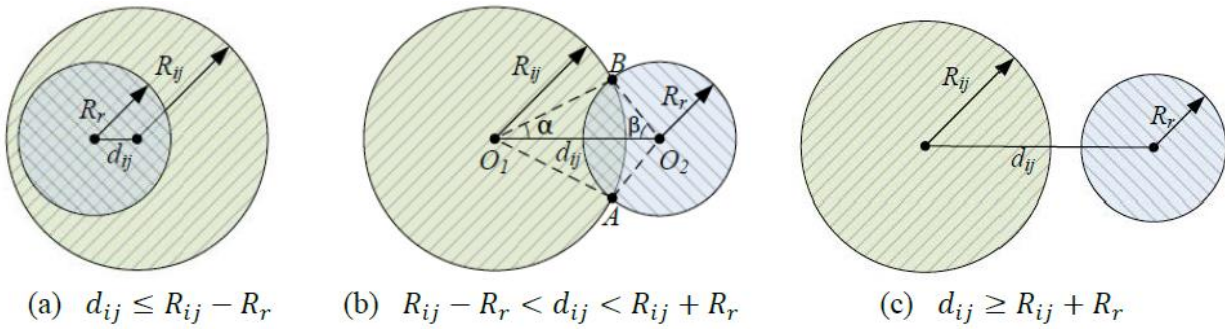547 <u>Figures</u>

548

549

550 **Figure 1**: Power and C_T curve for Vestas-V52 850 kW [29]

551 Note : To be reproduced in color on the Web and in black-and-white in print.

552

553

(a) $d_{ij} \leq R_{ij} - R_r$ (b) $R_{ij} - R_r < d_{ij} < R_{ij} + R_r$ (c) $d_{ij} \geq R_{ij} + R_r$

554

Figure 2 : Schematic view of affected area of turbines while considering wake effects under 3
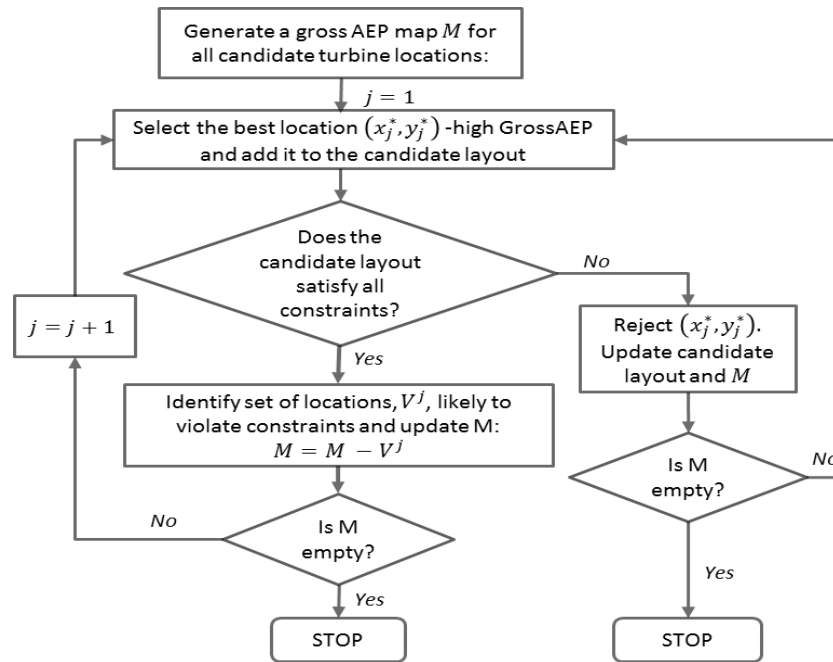
situations (a) full wake or complete wake, (b) partially wake, (c) out of wake [27].

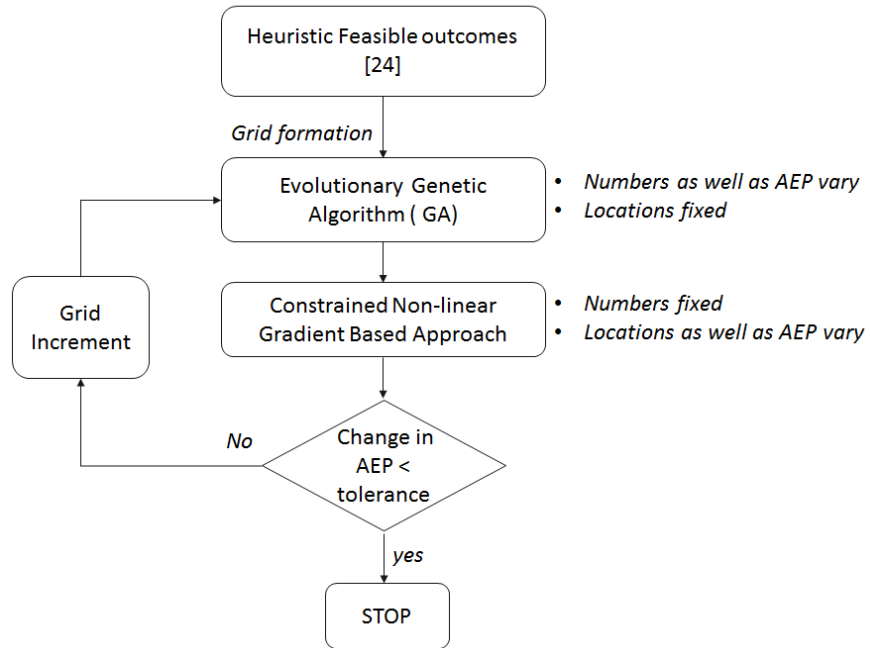Note : To be reproduced in color on the Web and in black-and-white in print.

558

559

Generate a gross AEP map M for all candidate turbine locations:

$j = 1$

Select the best location (x_j^*, y_j^*) -high GrossAEP and add it to the candidate layout

Does the candidate layout satisfy all constraints?

No

Reject (x_j^*, y_j^*). Update candidate layout and M

$j = j + 1$

Yes

Identify set of locations, V^j, likely to violate constraints and update M:
$M = M - V^j$

Is M empty?

No

No

Is M empty?

No

Yes

Yes

STOP

STOP

560

Figure 3: Flowchart of Heuristic approach [24]

561

32

562

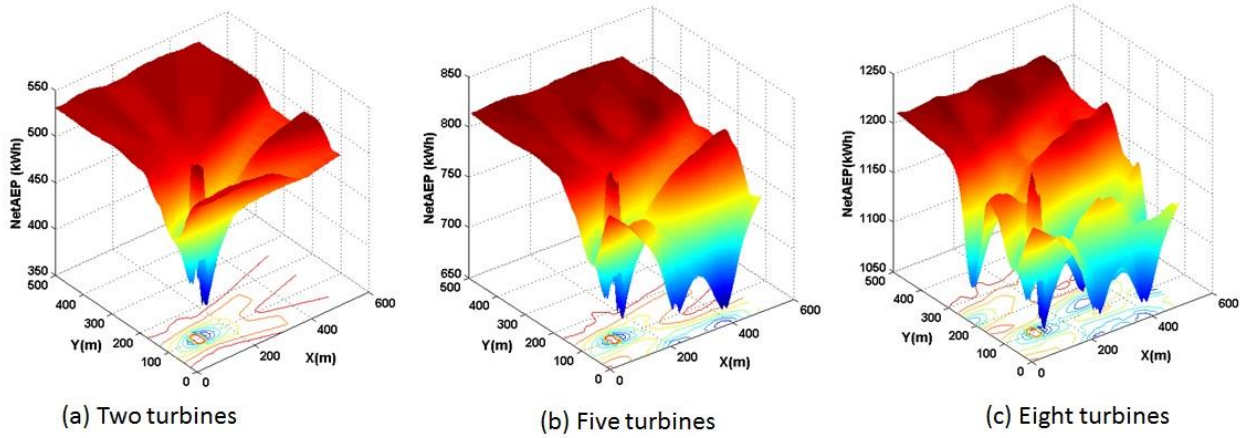**Figure 4**: Schematic Representation of Hybrid Methodology

563

564

565

Figure 5: Binary array and location index array at grid formation step.

566

567

568

34

569
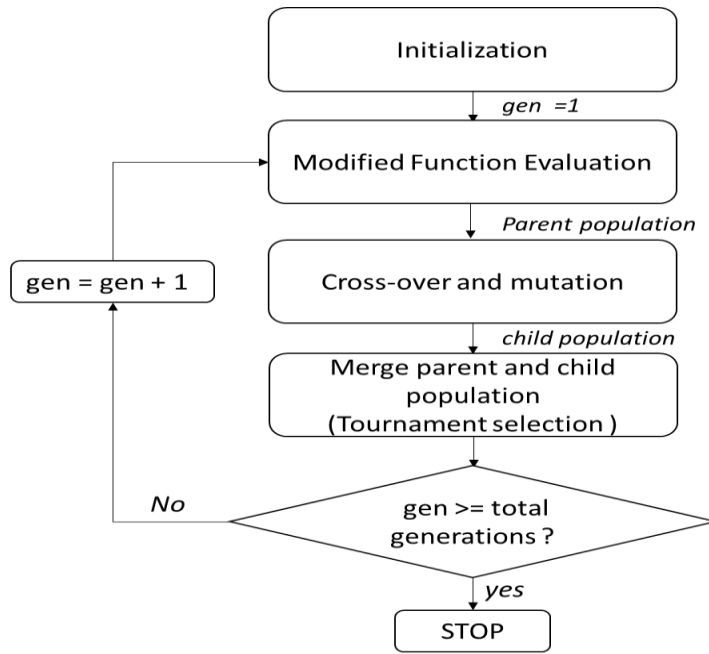
570

571   **Figure 6**: Flowchart of Evolutionary Algorithm

572

573

Figure 7: Population matrix formed at initialization step.

575

576

577

Figure 8: Formation of new index matrix after adding gradient outcomes in grid increment step.

578

579

580

581

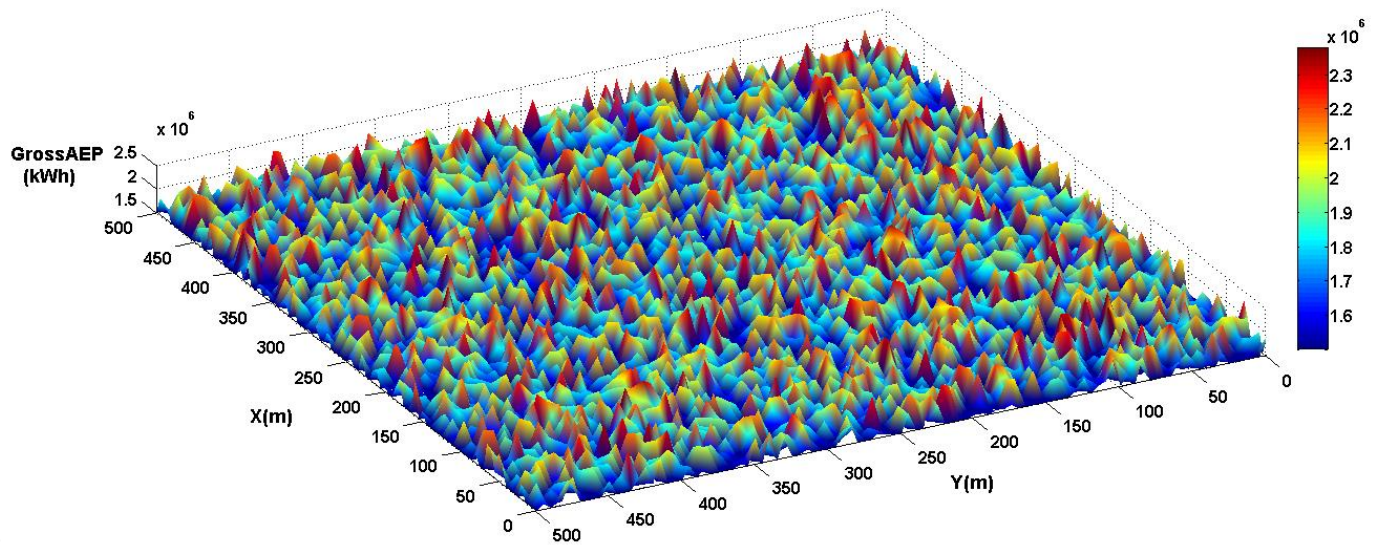(a) Two turbines   (b) Five turbines   (c) Eight turbines

582

Figure 9: Surface contour plot showing the distribution of net AEP over the given layout for 3

situations (a) two turbines (b) Five turbines (c) Eight turbines.

Note : To be reproduced in color on the Web and in black-and-white in print.

586

38

587

588

Figure 10: Type −I Gross AEP distribution over a given boundary.
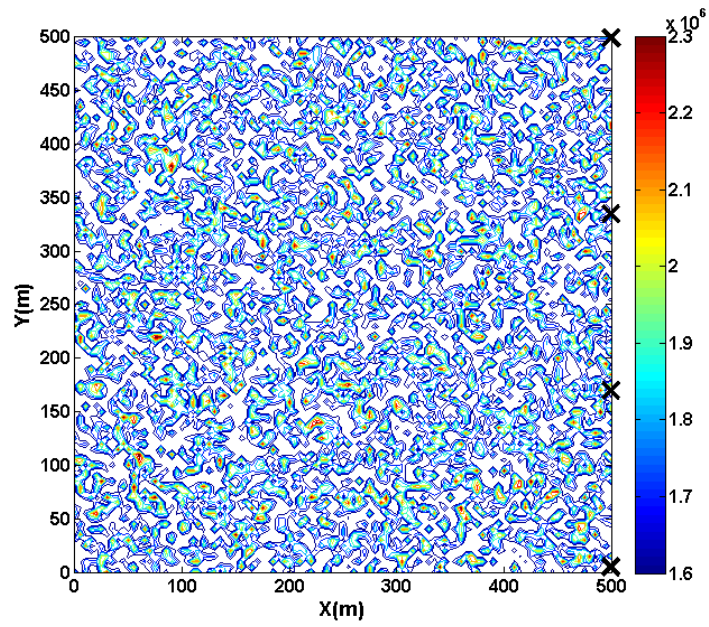
590   Note : To be reproduced in color on the Web and in black-and-white in print.

591

592

593

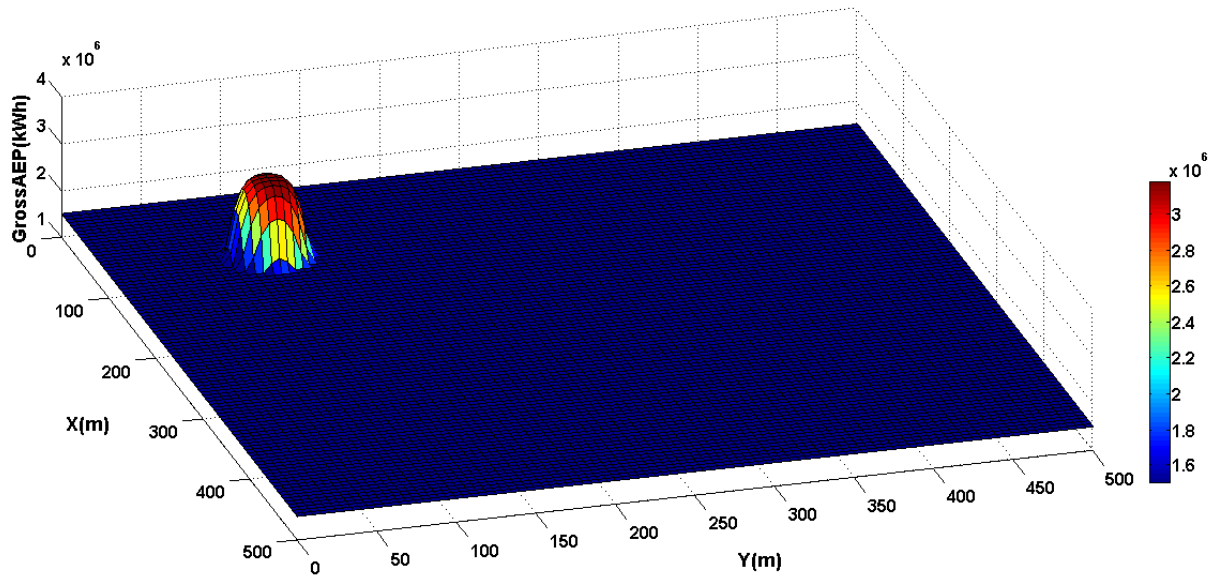**Figure 11**: Accepted turbines locations (black cross markers) superimposed on Type – I Gross

AEP contour plot of wind farm

Note : To be reproduced in color on the Web and in black-and-white in print.

597

598

599

Figure 12: Type –II Gross AEP distribution over a given boundary

601   Note : To be reproduced in color on the Web and in black-and-white in print.

602

603

(a) Case II   (b) Case III

604
605 **Figure 13**: Comparison of accepted turbines (black cross markers) superimposed on (a) Case II

606   (Type II Gross AEP plot) and (b) Case III (Type – III Gross AEP plot) of a wind farm.

607   Note : To be reproduced in color on the Web and in black-and-white in print.
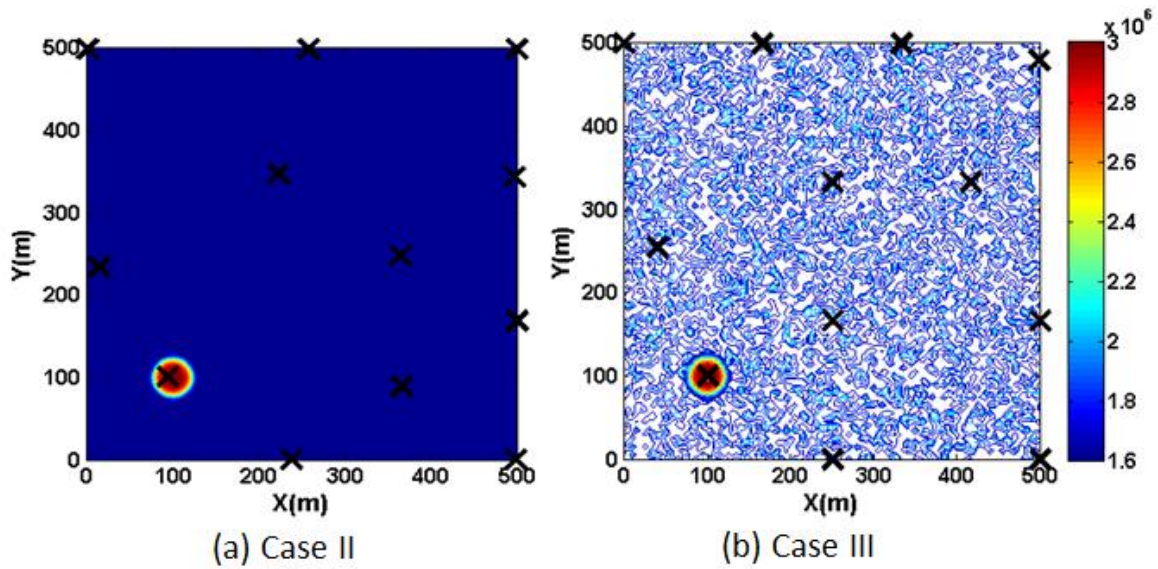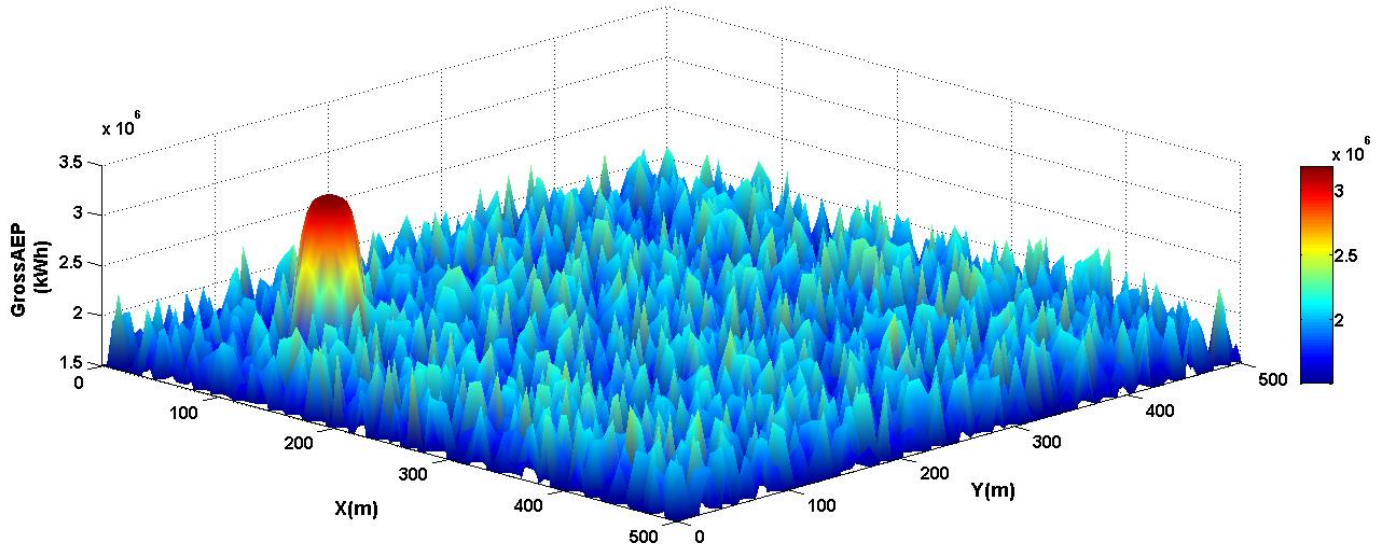
608

609

610

Figure 14: Type –III Gross AEP distribution over a given boundary

612   Note : To be reproduced in color on the Web and in black-and-white in print.

613

614

615
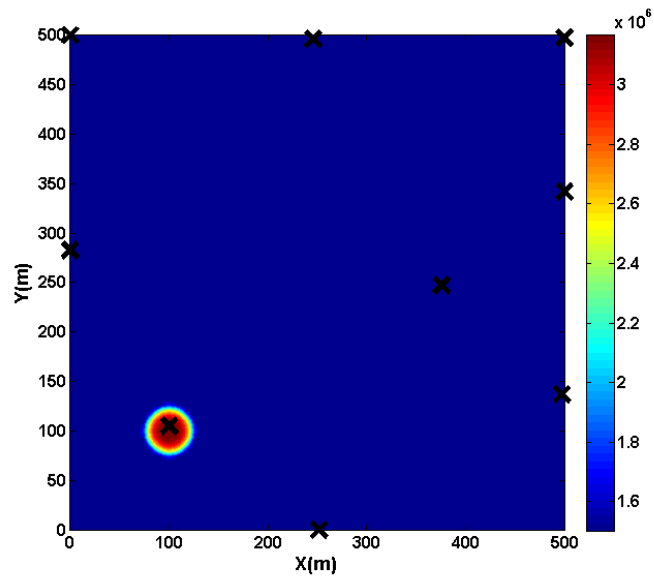
Figure 15: Accepted turbine locations (black cross markers) from binary- real coded GA

superimposed on Type – II Gross AEP contour plot.

Note : To be reproduced in color on the Web and in black-and-white in print.

619

620
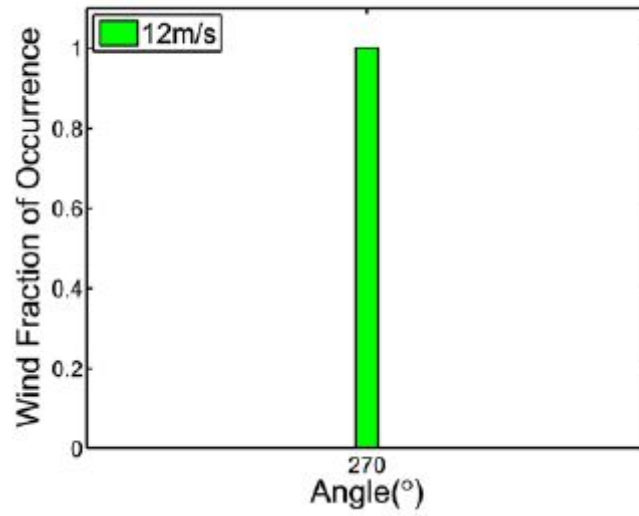
Figure 16 : Uniform wind distribution for case IV.

621
622

623   Note : To be reproduced in color on the Web and in black-and-white in print.

624

625
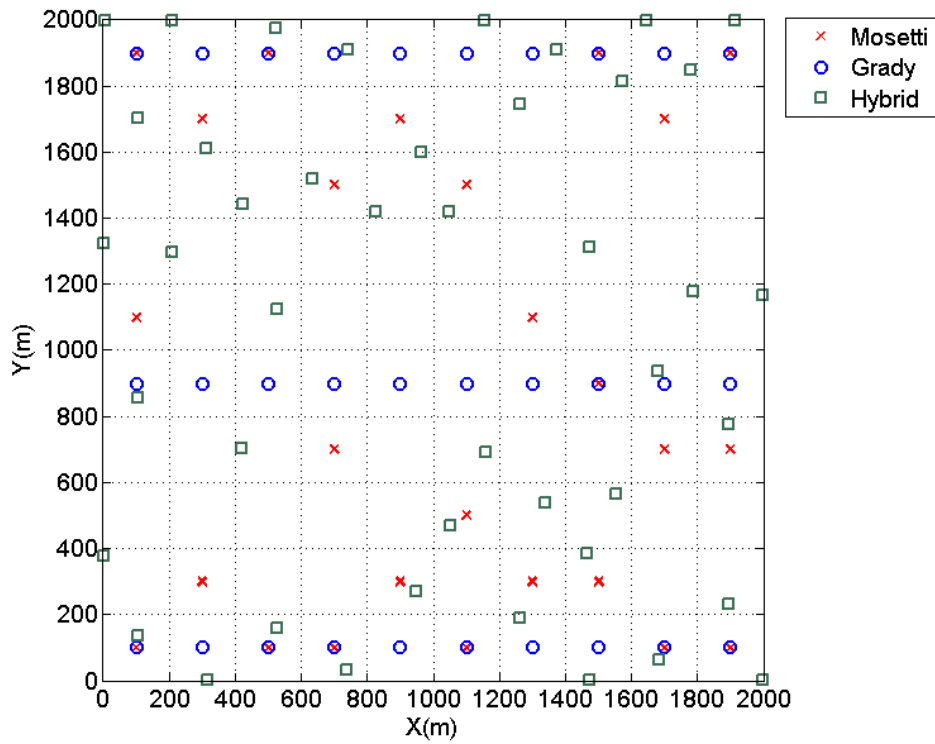
Figure 17 : Accepted turbine layouts for various methodologies (shown by different markers)
applied on Case study IV.

628

Note : To be reproduced in color on the Web and in black-and-white in print.

630

631

632 # <u>Tables</u>

633 **Table 1**: Parameters used in GA and Gradient based approach

Genetic Algorithm (MEGA) specifications	
Algorithm Type	Elitist-Tournament selection
Number of Population (n_{pop})	50
Number of Generations (n_{gen})	150
Crossover Probability	0.80
Crossover Type	Uniform
Mutation Probability	0.01
Gradient Based solver	
Solver	fmincon MATLAB®
Algorithm	Interior Point

634

635

636   **Table 2:** Wind farm, wind turbine and wake model specifications [24]

637

Wind farm Information	
Farm area (m^2)	500×500
Wind turbine specifications	
Turbine Type	Vestas V52-850 KW [29]
Turbine Rated Capacity (Pr) (kW)	850
Turbine Diameter (m)	52
Wake model Information	
Model	Jensen [25]
Jensen Constant (k_w)	0.075

638   **Table 3**: Outcome of hybrid methodology case 1

Cycle	Algorithm	Outcome	Number of turbines / feasible locations	AEP (Kwh)	Number of binaries
1	**Heuristic [24]**	H0	3	599.70	52
	MEGA	A1	4	626.67	
	Gradient	B1	4	651.96	
2	**MEGA**	A2	4	859.96	55
	Gradient	B2	4	865.95	
3	**MEGA**	A3	4	865.95	59
	Gradient	B3	4	865.95	

639

640

641 **Table 4: Outcome of hybrid methodology case II.**

642

Cycle	Algorithm	Outcome	Number of turbines / feasible locations	AEP (Kwh)	Number of binaries
1	**Heuristic [24]**	H0	8	1360.00	57
	MEGA	A1	10	1712.28	
	Gradient	B1	10	1765.33	
2	**MEGA**	A2	10	1789.96	67
	Gradient	B2	10	1803.83	
3	**MEGA**	A3	11	1921.74	77
	Gradient	B3	11	1941.28	
4	**MEGA**	A4	11	1941.54	88
	Gradient	B4	11	1943.26	
5	**MEGA**	A5	12	2046.92	99
	Gradient	B5	12	2054.29	
6	**MEGA**	A6	12	2054.35	111
	Gradient	B6	12	2054.43	

643

644

645

Table 5: Outcome of hybrid methodology case III.

Cycle	Algorithm	Outcome	Number of turbines / feasible locations	AEP (Kwh)	Number of binaries
1	**Heuristic [24]**	H0	9	1580.58	58
	MEGA	A1	9	1605.24	
	Gradient	B1	9	1607.71	
2	**MEGA**	A2	11	1978.64	62
	Gradient	B2	11	1978.64	
3	**MEGA**	A3	11	1996.68	66
	Gradient	B3	11	1996.68	
4	**MEGA**	A4	11	2058.81	67
	Gradient	B4	11	2058.81	

646

647 **Table 6:** Savings in expensive function evaluation by MEGA approach over EGA approach
648

Cycle	Function calls by EGA	Function calls saved by MEGA	% saved	Overall saved per case study
Case 1: Type – I Gross AEP distribution				
1	7550	1896	25.11	
2	7550	1580	20.92	22.75
3	7550	1679	22.23	
Case 2: Type – II Gross AEP distribution				
1	7550	3811	50.47	
2	7550	3356	44.45	
3	7550	3549	47.00	
4	7550	3940	52.18	51.85
5	7550	4307	57.04	
6	7550	4526	59.94	
Case 3: Type – III Gross AEP distribution				
1	7550	2899	38.39	
2	7550	2783	36.86	
3	7550	3033	40.17	38.85
4	7550	3018	39.97	

649

650
651 **Table 7:** Wind farm, wind turbine and wake model characteristics [8] for case IV.
652

653

654

Wind farm Information	
Farm area (m^2)	2000×2000
Wind turbine specifications	
Turbine Diameter (m)	40
Turbine Rated Power (Pr) (kW)	630
Hub Height (Z) (m)	60
Coefficient of Thrust (C_T)	0.88
Surface Roughness (Z$_0$) (m)	0.3
Wake model Information	
Model	Jensen [25]
Jensen Constant (k_w)	0.0944

655   **Table 8:** Comparison of various methodologies with present study for Case study IV.
656

	Mosetti et al. [8]	Grady et al. [9]	Wan et al. [12]	Present study	Chen et al. [23]
COST/ P_{tot}	0.0016197	0.0015436	0.0014475	**0.0014386**	0.0013456
Total Power (P_{tot}) (kW)	12352	14310	15262	**20742.54**	22624.3
Number of turbines	26	30	30	**44**	45

657

658 **Table 9:** Outcome of hybrid methodology on case IV.
659

660

Cycle	Algorithm	Outcome	Number of turbines / feasible locations	Fitness ratio(COST/P_{tot})
1	**MEGA**	A1	41	0.0014579
	Gradient	B1	41	0.0014505
2	**MEGA**	A2	43	0.0014496
	Gradient	B2	43	0.0014491
3	**MEGA**	A3	43	0.0014491
	Gradient	B3	43	0.0014470
4	**MEGA**	A4	43	0.0014470
	Gradient	B4	43	0.0014450
5	**MEGA**	A5	42	0.0014435
	Gradient	B5	42	0.0014428
6	**MEGA**	A6	42	0.0014428
	Gradient	B6	42	0.0014423
7	**MEGA**	A7	44	0.0014403
	Gradient	B7	44	0.0014386
8	**MEGA**	A8	44	0.0014386
	Gradient	B8	44	0.0014386

661